

# Allegheny Mountain



## Colloquium



**Speaker:** Dr. Stephen Deterding  
(West Liberty University)

**Date:** 7 February 2022, 4PM–5PM

**Zoom link:** <https://bit.ly/3qgbZNg>

**Title:** Pell's equation and the Chakravala method

**Abstract:**

In 1657 Pierre de Fermat issued a challenge to European mathematicians to find a positive integer solution to the equation  $61x^2 + 1 = y^2$ . However, unknown to him, this problem had been solved over 500 years earlier by an Indian mathematician named Bhaskara II using the Chakravala method. Fermat's challenge problem is an example of a type of equation known as Pell's equation, which is an equation of the form  $nx^2 + 1 = y^2$ , where integer solutions are sought for  $x$  and  $y$ . Pell's equation has important applications in approximating square roots because if  $x_1$  and  $y_1$  are a solution pair for Pell's equation then  $\frac{y_1}{x_1}$  is a very accurate approximation to  $\sqrt{n}$ . The Chakravala method was developed by Bhaskara II and others as a way to solve Pell's equation for all values of  $n$ . In this talk we will describe how the Chakravala method works and demonstrate its use in solving different forms of Pell's equation.

